B. C. A. (First Semester)

EXAMINATION, Dec., 2016

(New Course)

Paper Fifth

MATHEMATICS-I

Time: Three Hours [Maximum Marks: 75]

Note: Attempt questions from all Sections as directed.

Inst. The candidates are required to answer only in serial order. If there are many parts of a question, answer them in continuation.

Section-A

(Short Answer Type Questions)

Note: Attempt all questions from this Section. Each question carries 3 marks.

1. (A) Find cofactor of the elements of the first row of the determinant:

$$\begin{bmatrix} 2 & 3 & 5 \\ 4 & 1 & 0 \\ 6 & 2 & 7 \end{bmatrix}$$

(B) Find the rank of matrix:

$$\begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 7 \\ 3 & 6 & 10 \end{bmatrix}$$

(C) evaluate:

$$\lim_{x\to a} \frac{x^m - a^m}{x - a}$$

- (D) Write the statement of Rolle's theorem with suitable example.
- (E) By using Maclaurian's theorem expand".
- (F) Evaluate:

$$\int \sin(\log x) dx$$

(G) Show that:

$$F(I) = 1$$

- (H) Find the angle between A=2i+2j k and B=6i-3j+2k.
- (I) By using Leibnitz theorem find the rth differentiation of $x^3 \cos x$

(Long Answer Type Questions)

Note: Attempt any two questions. Each question carries 12 marks.

2. Use Cramer's rule to solve the following system of equations:

$$X - 4y - z = 11$$

$$2x - 5y + 2x = 39$$

$$-3x + 2y + z = 1$$

3. Find the Eigen values and the corresponding Eigen vector for the following matrix:

$$\begin{bmatrix} 1 & 1 & -2 \\ -i & 2 & 1 \\ 0 & i & -i \end{bmatrix}$$

4. Examine for continuity at the origin of function:

$$f(x) = \begin{cases} \frac{x - [x]}{x} & \text{if } x \neq 0 \\ 1 & \text{if } x = 0 \end{cases}$$

5. Differentiate the following w. r. to x.:

$$(i) e^3 + \log_e x + a^3$$

(ii)
$$\cos(\cot x^2)$$

(iii)
$$x\sqrt{x}$$

Section C

(Long Answer Type Questions)

Note: Attempt any two questions. Each question carries 12 marks.

6. (a) If f(x) = (x - 1)(x - 2)(x - 3) and a = 0, b = 4, find e using Lagrange's mean value theorem.

- (b) Expand sin x in power of $(x \frac{x}{2})$ by using Taylor's series.
- 7. (a) Find the maximum and minimum value of the function $f(x) = x^3 2x^2 + x + 6$
- (b) By using L'Hospital rule evaluate:

$$\lim_{x\to\infty}\frac{x^3}{e^x}$$

8. Evaluate the following integral function:

(i)
$$\int \sin^3 x \cos x \, dx$$

(ii)
$$\int_0^1 \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx$$

9. (a) Show that:

$$\int_0^{\pi/6} \cos^6 3\theta \, \sin^2 6\theta \, d\theta = \frac{7\pi}{384}$$

(b) Show that three vectors 2i + 6j + 7k, 7i - 8j + 9k and 3i + 20j + 5k are collinear.